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Amalgamations of commutative feebly clean-like rings

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Abstract

We investigate the transfer of the feebly clean, feebly J -clean, and feebly nil-clean rings in the amalgamated algebras along an ideal. We put the transfer results in use to provide examples subject to the involved ring theoretic notions as well as to recover some previous results related to the transfer of these notions in other constructions such as trivial ring extension.

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Ethics declarations

Conflicts of interest

The authors have no conflicts of interest to declare. The co-authors has seen and agree with the contents of the manuscript and there is no financial interest to report. We certify that the submission is original work and is not under review at any other publication.

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